

## Electron Spin Resonance of X-Irradiated Single Crystals of Zinc Acetate Dihydrate: Hindered Rotation of Methylene Group in a Free Radical $\text{CH}_2\text{COO}^{\cdot-}$ \*

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Electron spin resonance spectra of X-irradiated single crystals of zinc acetate dihydrate have been studied at 9.2 Gc in the temperature range from 77°K to 380°K. The radicals trapped at 77°K are  $\text{CH}_3$  and  $\text{CH}_2\text{COO}^{\cdot-}$ . The former disappears above 150°K. The latter is stable and persists up to 370°K. The principal values of hyperfine coupling constants for two inequivalent hydrogens of the radical  $\text{CH}_2\text{COO}^{\cdot-}$  have been found to be 10.5, 20.6 and 33.4 G. The  $\text{CH}_2$  group in the radical undergoes restricted rotation about the C—C bond. Analysis of the ESR spectra at different temperatures with a modified Bloch equation shows the activation energy and the frequency factor for the restricted rotation to be  $5.8 \pm 0.2$  kcal/mol and  $(4.4 \pm 2.7) \times 10^{12}$  sec<sup>-1</sup>, respectively.

Electron spin resonance (ESR) studies of free radicals have given valuable information on the structure of the radicals as well as their restricted motion. Changes in ESR spectra with temperature due to motion of free radicals have been found and analyzed in some irradiated organic substances. Methyl groups undergo restricted reorientation about a C—C bond in such radicals as  $\text{CH}_3\text{CHCOOH}$  trapped in alanine<sup>1,2)</sup> and  $\text{CH}_3\text{C}(\text{COOH})\text{CH}_2\text{COOH}$  trapped in itaconic acid<sup>3)</sup>. Their rotation is nearly quenched below 100°K, but the methyl group of a radical  $\text{CH}_3\text{C}(\text{COOH})_2$  in irradiated malonic acid executes nearly free rotation even at 4.2°K.<sup>4)</sup> Restricted torsional motion of a methylene group about a C—C bond has also been found in radicals trapped in an irradiated crystal of hexamethylenediammonium adipate,<sup>5)</sup> in an irradiated mixed crystal of urea-fumaric acid<sup>6)</sup> and in irradiated ethylmalonic acid and *n*-propylmalonic acid.<sup>7)</sup> Reorientation of a terminal methylene group, however, has not been found in a radical of the type  $\text{CH}_2\text{R}$  within the knowledge of the present authors, except insufficient evidence for the reorientation motion in a radical

$\text{CH}_2\text{COO}^{\cdot-}$  trapped in an irradiated crystal of glycine.<sup>8)</sup>

In this paper, the ESR studies of X-irradiated single crystals of zinc acetate dihydrate  $\text{Zn}(\text{CH}_3\text{COO})_2 \cdot 2\text{H}_2\text{O}$  are presented. The trapped radicals have been identified as  $\text{CH}_3$  and  $\text{CH}_2\text{COO}^{\cdot-}$ . A marked temperature dependence has been found in the absorption spectra of the radical  $\text{CH}_2\text{COO}^{\cdot-}$ , from which it is concluded that the motion of the  $\text{CH}_2$  group is quenched at low temperatures but undergoes rapid reorientation around the C—C bond above room temperatures. A quantitative analysis of the temperature dependence of the ESR spectra has been undertaken to give the activation energy and the frequency factor for the internal rotation of the radical in the crystal.

### Experimental Procedures and Outline of the ESR Spectra

Single crystals of zinc acetate dihydrate were grown from the aqueous solution by slow evaporation. The crystal structure has been determined by Niekerk *et al.*<sup>9)</sup>; the lattice is monoclinic with space group  $C2/c-C_{2h}^6$ ,  $a=14.5$ ,  $b=5.32$ ,  $c=11.02$  Å and  $\beta=100.0^\circ$  with four molecules per unit cell. The crystal axes were determined by comparing interfacial angles calculated from the lattice constants with those observed with an optical goniometer available from the Stoe Co. An orthogonal

\*<sup>1</sup> Presented at the 5th Symposium on Electron Spin Resonance, Sendai, Sept., 1966.

<sup>1</sup>) I. Miyagawa and K. Itoh, *J. Chem. Phys.*, **36**, 2157 (1962).

<sup>2</sup>) A. Horsfield, J. R. Morton and D. H. Whiffen, *Mol. Phys.*, **5**, 115 (1962).

<sup>3</sup>) M. Fujimoto, *J. Chem. Phys.*, **39**, 846 (1963).

<sup>4</sup>) C. Heller, *ibid.*, **36**, 175 (1962).

<sup>5</sup>) M. Kashiwagi and Y. Kurita, *ibid.*, **39**, 3165 (1963).

<sup>6</sup>) C. Corvaja, *ibid.*, **44**, 1958 (1966).

<sup>7</sup>) N. Tamura, M. A. Collins and D. H. Whiffen, *Trans. Faraday Soc.*, **62**, 1037 (1966); *ibid.*, **62**, 2434 (1966).

<sup>8</sup>) R. F. Weiner and W. S. Koski, *J. Am. Chem. Soc.*, **85**, 873 (1963); J. R. Morton, *ibid.*, **86**, 2325 (1964).

<sup>9</sup>) J. N. van Niekerk, F. R. L. Schoening and J. H. Talbot, *Acta Cryst.*, **6**, 720 (1953).

10) M. T. Rogers and L. D. Kispert, *J. Chem. Phys.*, **46**, 221 (1967).

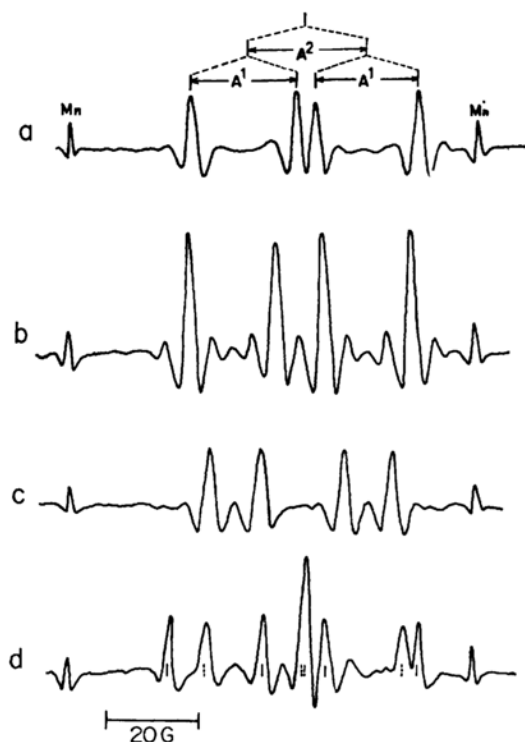


Fig. 3. Second derivative spectra of the crystal irradiated at room temperature and measured at 77°K with the magnetic field (a) parallel to the  $a$  axis, (b) parallel to the  $b$  axis, (c) parallel to the  $c$  axis and (d) at an angle of 30° from the  $a$  axis toward the  $b$  axis in the  $ab$  plane. The outermost lines are of  $Mn^{2+}$  in  $MgO$  powder which is used as field marker (spacing; 87.5 G).

is parallel to the  $b$  axis or in the  $ac'$  plane. The same spectra were obtained when the direction of the field is  $(l, m, n)$  or  $(l, -m, n)$ , where  $l, m$  and  $n$  are the direction cosines of the magnetic field with respect to the  $abc'$  system. These facts are compatible with the expectation that the two chemically equivalent but magnetically different radicals are trapped in the crystal with monoclinic symmetry.

It is evident that each quartet arises from two protons with different nuclear hyperfine coupling constants which are referred to as  $A^1$  and  $A^2$  as shown in Fig. 3. Figure 4 shows angular dependences of  $A^1$  and  $A^2$  observed when the magnetic field is in the  $ab$ ,  $bc'$  or  $ac'$  planes. The observed data were analyzed by means of least mean square method with the aid of the second-order equations. The calculation was performed by an electronic computer. Table 1 shows the values determined for the principal elements of the tensors  $A^1$  and  $A^2$ , and those of the spectroscopic splitting tensor  $g$ . The angular dependences of  $A^1$  and  $A^2$  calculated from the results given in Table 1 are shown gra-

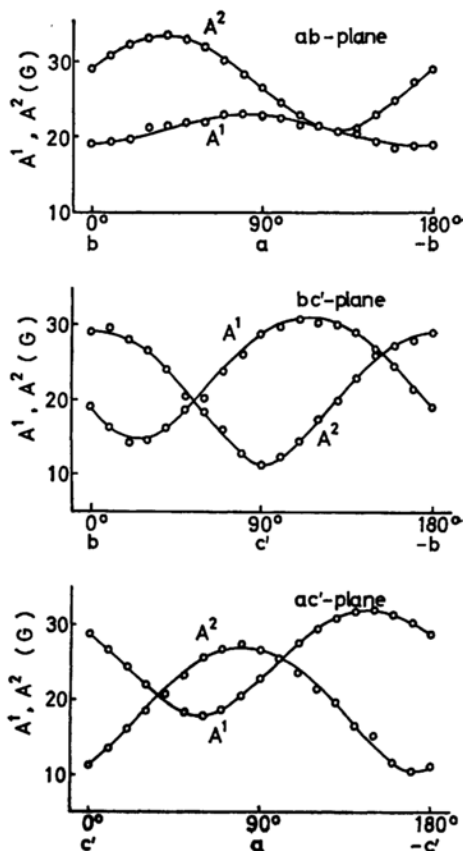
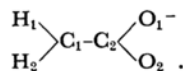


Fig. 4. Calculated (solid lines) and observed (circles) hyperfine splittings at low temperature with the magnetic field in the  $ab$ ,  $bc'$  and  $ac'$  planes in a single crystal of zinc acetate dihydrate irradiated at room temperature. The angular dependences of  $A^1$  and  $A^2$  are illustrated for one of the two quartets observed with the magnetic field in the  $ab$  and  $bc'$  planes. A 180° rotation of the curves illustrated in the figure about the  $b$  axis gives the curves omitted.

phically in Fig. 4. The principal values of  $A^1$  and  $A^2$  are identical within the limit of experimental error. Therefore, the radical responsible for the spectrum R must contain  $CH_2$  and is most likely



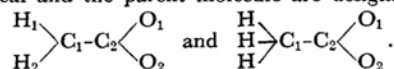
Further analysis confirms this identification. An unpaired electron is in the  $p_x$  orbital of the  $sp^2$  configuration of  $C_1$ . In such a radical, it has been shown both theoretically and experimentally that the smallest  $g$  value ( $g_1$ ) should occur along the direction parallel to the symmetry axis of the  $p_x$  orbital (perpendicular to the radical plane) and the directions corresponding to the minimum, medium and maximum value of the principal elements of the hfs tensor are parallel to the C-H bond, parallel

TABLE 2. THE ORIENTATION OF THE RADICAL  $\text{CH}_2\text{COO}^-$  AND THE PARENT MOLECULE  $\text{CH}_3\text{COO}^-$  IN A CRYSTAL OF ZINC ACETATE DIHYDRATE<sup>a)</sup>

Direction	Vector <sup>b)</sup>	Direction cosine with respect to the $abc'$ system <sup>c, d)</sup>			
$\text{C}_1\text{-C}_2$ (radical)	$(\mathbf{A}_1^1 + \mathbf{A}_2^1)$	0.592	0.675	-0.443	$(\mathbf{n}_{r1})$
	$\mathbf{g}_3$	0.641	0.449	-0.583	$(\mathbf{n}'_{r1})$
$\text{C}_1\text{-C}_2$ (molecule)	From crystal structure <sup>b)</sup>	0.662	0.534	-0.531	$(\mathbf{n}_{m1})$
Normal to the plane of $\text{H}_1\text{H}_2\text{O}_1\text{O}_2$ (radical)	$(\mathbf{A}_1^1 \times \mathbf{A}_2^1)$	0.792	-0.588	0.165	$(\mathbf{n}_{r2})$
	$\mathbf{g}_1$	0.726	-0.639	0.252	$(\mathbf{n}'_{r2})$
Normal to the plane of $\text{O}_1\text{O}_2\text{C}_1\text{C}_2$ (molecule)	From crystal structure <sup>b)</sup>	0.892	-0.446	0.115	$(\mathbf{n}_{m2})$

The angle between  $\text{C}_1\text{-C}_2$  (radical) and  $\text{C}_1\text{-C}_2$  (molecule) is  $9^\circ$  ( $\angle \mathbf{n}_{m1}, \mathbf{n}_{r1}$ ) or  $13^\circ$  ( $\angle \mathbf{n}_{m1}, \mathbf{n}'_{r1}$ ). The angle between the normal to the plane of  $\text{H}_1\text{H}_2\text{O}_1\text{O}_2$  (radical) and that of  $\text{O}_1\text{O}_2\text{C}_1\text{C}_2$  (molecule) is  $9^\circ$  ( $\angle \mathbf{n}_{m2}, \mathbf{n}_{r2}$ ) or  $16^\circ$  ( $\angle \mathbf{n}_{m2}, \mathbf{n}'_{r2}$ ).

a) The atoms in the radical and the parent molecule are designated as;



b)  $\mathbf{A}_1^1$ ,  $\mathbf{A}_2^1$ ,  $\mathbf{g}_3$  and  $\mathbf{g}_1$  represent the principal vectors shown in Table 1.

c) Of the two crystallographically unequivalent species, direction cosines are tabulated for one species.

d) Unit vectors having these direction cosines are designated as  $\mathbf{n}_{r1}$ ,  $\mathbf{n}'_{r1}$ , etc.



Fig. 5. Observed (solid lines) and calculated (dotted lines) second derivative ESR spectra of  $\text{CH}_2\text{COO}^-$  in the crystal for the magnetic field parallel to the  $c$  axis at different temperature  $T$ . The calculated spectra are obtained according to Eq. (2) together with Eq. (3) and the values of  $E$  and  $f_0$  indicated in (4).

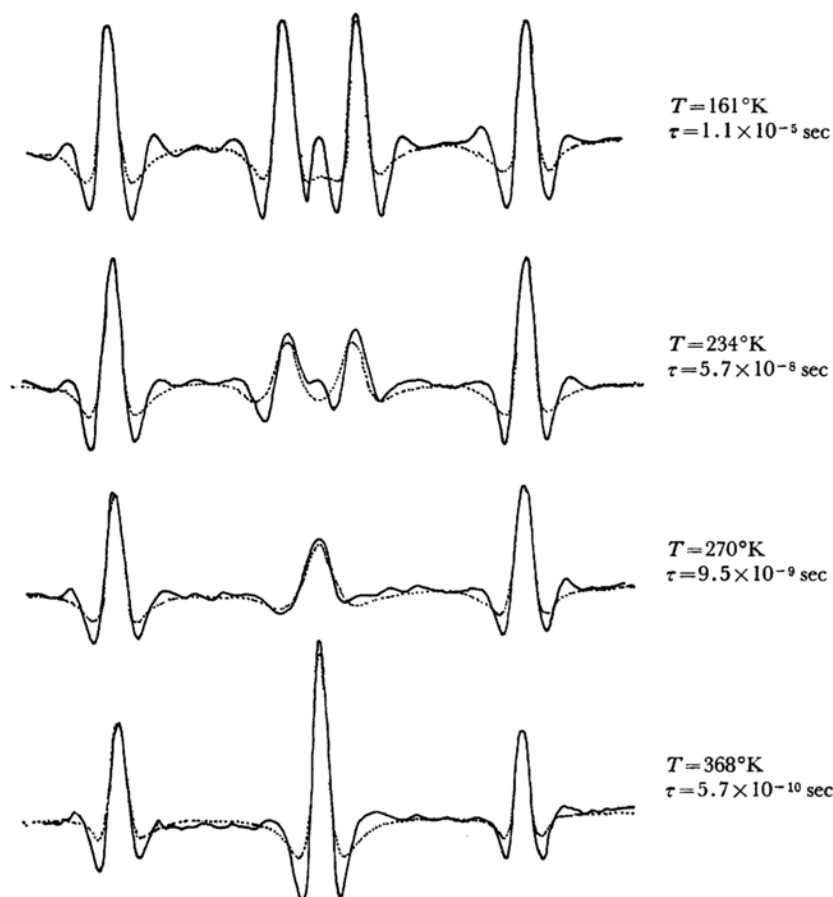


Fig. 6. Second derivative absorption curves of  $\text{CH}_2\text{COO}^-$  similar to Fig. 5, except that the applied magnetic field is in the  $ac'$  plane and makes an angle of  $23^\circ$  with the  $a$  axis toward the  $c'$  axis.

to the symmetry axis of the  $p_x$  orbital and perpendicular to these two directions, respectively.<sup>11-13)</sup>

In addition, a symmetry consideration on the radical predicts that the direction of the  $\text{C}_1\text{-C}_2$  bond is parallel to a bisector of the directions of the minimum principal values of  $\mathbf{A}^1$  and  $\mathbf{A}^2$  or is parallel to  $\mathbf{g}_2$  or  $\mathbf{g}_3$ , where  $\mathbf{g}_2$  and  $\mathbf{g}_3$  are the medium and maximum principal elements of  $\mathbf{g}$  tensor, respectively.

The direction of the  $\text{C}_1\text{-C}_2$  bond and the normal to the plane  $\text{H}_1\text{C}_1\text{C}_2\text{H}_2$  of the radical are determined from the values given in Table 1 and compared with the orientation of the parent molecule in the crystal which is determined by X-ray analysis.<sup>9)</sup> The direction normal to the plane  $\text{H}_1\text{C}_1\text{C}_2\text{H}_2$  (perpendicular to  $\mathbf{A}_1^1$  and  $\mathbf{A}_1^2$ ) agrees within  $8^\circ$  with the direction along the symmetry axis of  $p_x$  orbital (parallel to  $\mathbf{g}_1$ ). The angle

$\angle \text{H}_1\text{C}_1\text{H}_2$  (angle between  $\mathbf{A}_1^1$  and  $\mathbf{A}_1^2$ ) is obtained as  $118^\circ \pm 3^\circ$ . As shown in Table 2, the direction of the  $\text{C}_1\text{-C}_2$  bond of the radical agrees with that of the parent molecule. Moreover, the plane  $\text{H}_1\text{C}_1\text{C}_2\text{H}_2$  of the radical is parallel to the plane  $\text{O}_1\text{O}_2\text{C}_1\text{C}_2$  of the parent molecule. These facts indicate that the free radical is formed from the parent molecule  $\text{CH}_3\text{COO}^-$  by loss of a hydrogen atom followed by a reorientation of the  $\text{CH}_2$  group to make a planar radical. The orientation of  $\text{O}_1\text{O}_2\text{C}_2$  is unchanged when the loss of hydrogen occurs. The principal values of the hfs tensor of the radical  $\text{CH}_2\text{COO}^-$  trapped in a zinc acetate dihydrate crystal (10.4, 20.8, 33.4G) are nearly equal to those of the radical  $\text{CH}_2\text{COO}^-$  produced in glycine (10.3, 21.8, 32.5G),<sup>14)</sup> and to those of  $\text{CH}_2\text{COOH}$  produced in malonic acid (11.9, 20.5, 32.6G).<sup>15)</sup> It is concluded that the spin density on the  $\alpha$ -carbon atom in these radicals is

11) H. M. McConnell, C. Heller, T. Cole and R. W. Fessenden, *J. Am. Chem. Soc.*, **82**, 766 (1960).

12) H. M. McConnell and R. E. Robertson, *J. Phys. Chem.*, **61**, 108 (1957).

13) H. M. McConnell and J. Strathdee, *Mol. Phys.*, **2**, 129 (1959).

14) H. C. Box, H. G. Freund and E. E. Budinski, *J. Am. Chem. Soc.*, **88**, 658 (1966).

15) A. Horsfield, J. R. Morton and D. H. Whiffen, *Nature*, **189**, 481 (1961).



Fig. 7. Temperature dependences of the first (left side) and second (right side) derivative ESR spectra of  $\text{CH}_2\text{COO}^-$  trapped in X-irradiated zinc acetate dihydrate powder. The value of  $\tau$  given in each spectrum is calculated from Eq. (3) with  $E$  and  $f_0$  indicated in (4).

unaffected whether the  $\text{COO}$  group is linked with neighboring molecules by hydrogen bonds or makes ionic bonds with  $\text{Zn}^{2+}$ .

#### Temperature Dependence of ESR Spectra; The Hindered Rotation of $\text{CH}_2$ Group of $\text{CH}_2\text{COO}^-$

Figures 5 and 6 show the ESR spectra of  $\text{CH}_2\text{COO}^-$  recorded at various temperatures with the magnetic field in the  $ac'$  plane. In the temperature range from 77°K to 170°K the spectrum is composed of a quartet with equal intensity. At higher temperatures, the outer lines of the quartet are unchanged, whereas the inner lines become broadened, their peak heights decrease, and their separation also decreases. Near 270°K the inner lines practically disappear. At higher temperature a line appears at the center of outer lines and its intensity increases with increase of temperature and approaches twice the intensity of the outer lines. First and second derivative ESR spectra of  $\text{CH}_2\text{COO}^-$  trapped in zinc acetate dihydrate

powder obtained at different temperatures are illustrated in Fig. 7 for comparison with the crystal ESR spectra.

The temperature dependence mentioned above is characteristic of the system in which the two hydrogen atoms exchange their sites with each other through a rotation of the  $\text{CH}_2$  group about the C-C bond, the rate of the exchange increasing with increasing temperature. This is easily recognized qualitatively as illustrated in Fig. 8. If the reorientation rate,  $\tau^{-1}$ , is much smaller than  $|A^\alpha - A^\beta|$ , the spectrum will be a quartet, where  $A^\alpha$  and  $A^\beta$  are the hyperfine coupling constants in frequency unit of the protons located at equilibrium positions " $\alpha$ " and " $\beta$ ", respectively. The resonant frequencies of the quartet are  $\nu_0 \pm |A^\alpha + A^\beta|/2$  (outer lines), corresponding to the nuclear spin states  $(++)$  and  $(--)$  of the two protons  $\text{H}_1$  and  $\text{H}_2$ , and  $\nu_0 \pm |A^\alpha - A^\beta|/2$  (inner lines), corresponding to  $(+-)$  and  $(-+)$ , where  $\nu_0$  is the resonant frequency of the unpaired electron with no hfs and  $(+-)$ , for example, designates the state in which  $\text{H}_1$  and  $\text{H}_2$  have nuclear spin components of  $+1/2$  and  $-1/2$ , respectively.

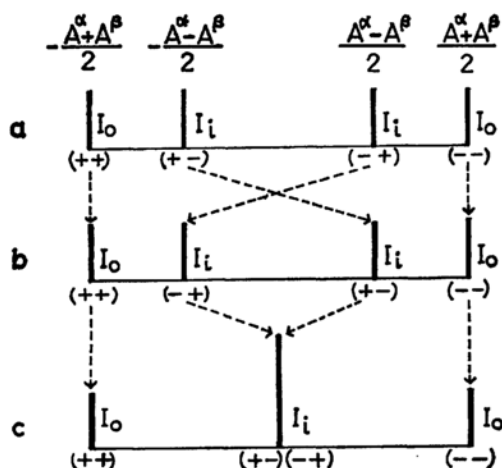


Fig. 8. Patterns of absorption spectra of  $\text{CH}_1\text{H}_2\text{R}$ .

- $\text{H}_1$  and  $\text{H}_2$  are in the equilibrium positions " $\alpha$ " and " $\beta$ ", respectively.
- $\text{H}_1$  and  $\text{H}_2$  exchanges their positions through rotation around the C-C bond.  $\text{H}_1$  and  $\text{H}_2$  are in " $\beta$ " and " $\alpha$ ", respectively.
- The methylene group undergoes rapid reorientation.

The relation  $A^\alpha > A^\beta > 0$  is assumed.

When  $\tau^{-1} \gg |A^\alpha - A^\beta|$ , the spectrum is a triplet with the intensity ratio of 1 : 2 : 1, the resonant frequencies of which are  $\nu_0 \pm |A^\alpha + A^\beta|/2$ , corresponding to  $(++)$  and  $(--)$ , and  $\nu_0$  which corresponds to  $(+-)$  and  $(-+)$ . If  $\tau^{-1}$  is comparable to  $|A^\alpha - A^\beta|$ , the positions and intensities of the outer lines are the same as those in the two cases mentioned above but inner lines become broadened and its separation becomes smaller than  $|A^\alpha - A^\beta|$ . These changes of the spectra with change of  $\tau^{-1}$  is caused by the fact that the nuclear spin state of the protons is unchanged during the reorientation and, then, the inner lines exchange their positions with each other but the outer lines do not through the reorientation. The exchange or reorientation effects of protons on NMR spectra have been analyzed by Gutowsky and Holm<sup>16)</sup> with modified Bloch equations. The effects of rotation of methyl group in a radical  $\text{CH}_3\text{CHR}$  on ESR spectra have been investigated with a similar procedure by Miyagawa and Itoh.<sup>1)</sup> After their procedure, we analyzed numerically the second derivative ESR spectra of a radical with two protons which transfer between two sites.

If the splitting of the inner lines  $H_{\text{spl}}(|A^\alpha - A^\beta|$  in gauss) and the maximum slope line width

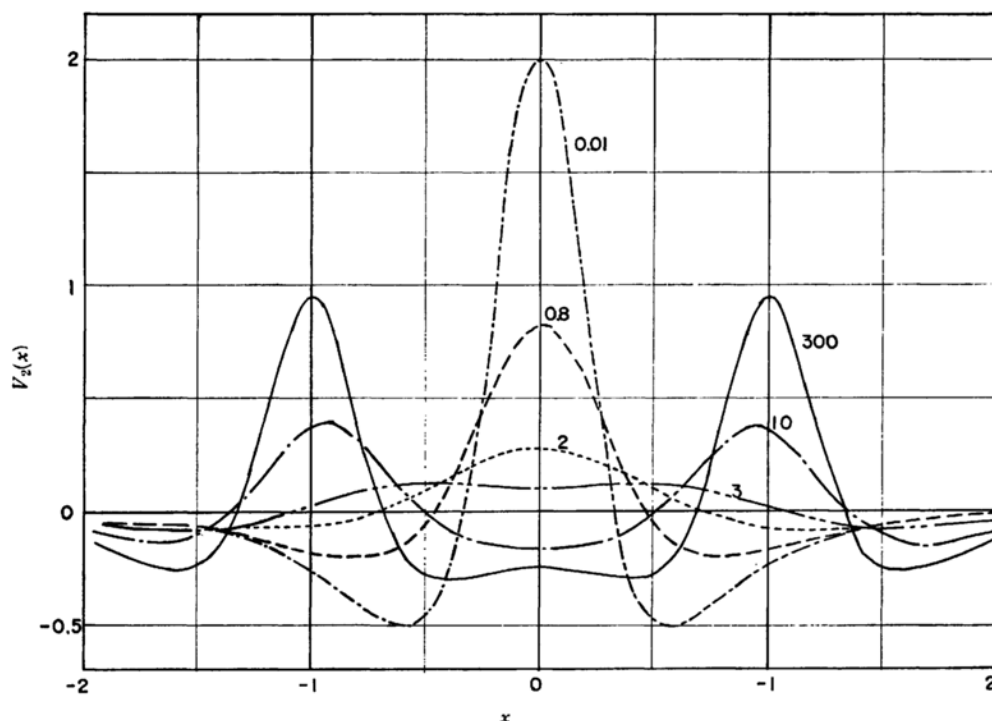


Fig. 9. Second derivative curves  $V_2(x)$  for  $r=0.33$  with different reduced exchange rates  $t$ . The values of  $t$  are given on each curves.

16) H. S. Gutowsky and C. H. Holm, *J. Chem. Phys.*, **25**, 1228 (1956); see also, J. A. Pople, W. G. Schneider and H. J. Bernstein, "High-Resolution

Nuclear Magnetic Resonance," McGraw-Hill Book Company, Inc., New York (1959), Chapt. 10.

$\Delta H_{\text{msl}}$ , both in the absence of the reorientation, are known, the spectra of the inner lines can be calculated for any given life time of the reorientation,  $\tau$ . The absorption curve,  $V_0$ , is given as a function of reduced magnetic field  $x$  by the expression

$$V_0(x) = \frac{\sqrt{3}}{2} \tau \text{Real} \left\{ \frac{f_\alpha + f_\beta}{1 - f_\alpha - f_\beta} \right\}, \quad (1)$$

and the second derivative of the absorption curves by

$$V_2(x) = \frac{3\sqrt{3}}{8} (\tau)^3 \times \text{Real} \left\{ \frac{(f_\alpha - f_\beta)^2 (f_\alpha + f_\beta - f_\alpha f_\beta) + f_\alpha f_\beta (f_\alpha + f_\beta)}{(1 - f_\alpha - f_\beta)^3} \right\} \quad (2)$$

where  $f_\alpha$  and  $f_\beta$  are complex functions expressed as

$$\left. \begin{aligned} f_\alpha &= \left\{ \frac{\sqrt{3}}{2} \tau t + 2 - i \frac{t}{2} (1 - x) \right\}^{-1} \\ f_\beta &= \left\{ \frac{\sqrt{3}}{2} \tau t + 2 + i \frac{t}{2} (1 + x) \right\}^{-1} \end{aligned} \right\} \quad (3)$$

$(i = \sqrt{-1})$

where

$$x = \frac{2}{H_{\text{spl}}} (H - H_0),$$

$$r = \Delta H_{\text{msl}} / H_{\text{spl}},$$

and

$$t = \tau \gamma H_{\text{spl}}.$$

In the above expressions,  $H$  is applied magnetic field,  $H_0$  is magnetic field at the center of the inner doublet and  $\gamma$  is electronic gyromagnetic ratio.

Line shape of each absorption line has been assumed to be Lorentzian and, therefore,  $\Delta H_{\text{msl}} = 2/(\sqrt{3} \gamma T_2)$ , where  $T_2$  is spin-spin relaxation time. Equations (1) and (2) are normalized so as  $V_0(\pm 1) = V_2(\pm 1) = 1$  when  $\tau = \infty$ . The maximum value of  $V_2(x)$  is the ratio of the peak intensity of the inner line,  $I_i$ , to that of the outer line,  $I_o$ , which can be calculated from Eq. (2) as a function of  $\tau$  for given  $r$  and  $H_{\text{spl}}$ .

At 77°K,  $\tau$  is large enough to assume that the rotation of the  $\text{CH}_2$  group of the radical  $\text{CH}_2\text{COO}^-$  does not take place practically and hence the linewidth and the separation between inner lines observed at this temperature can be taken as  $\Delta H_{\text{msl}}$  and  $H_{\text{spl}}$ , respectively. The values of  $H_{\text{spl}}$  and  $\Delta H_{\text{msl}}$  have been observed to be 20.1 G and 2.52 G ( $r=0.125$ ), respectively, for  $H$  parallel to the  $c$  axis, and to be 8.1 G and 2.67 G ( $r=0.33$ ), respectively, for the magnetic field parallel to a line which makes an angle of  $+23^\circ$  with the  $a$  axis in the  $ac'$  plane. Figure 9 shows the calculated spectra of the inner lines for several values of  $t$

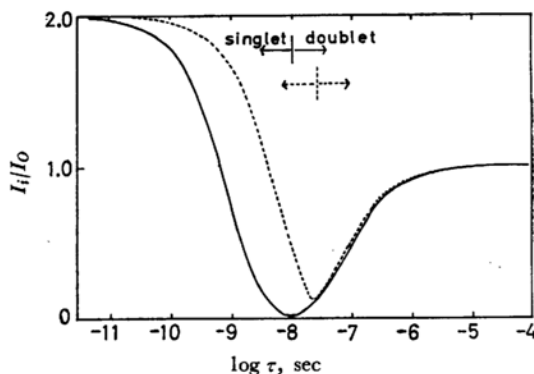


Fig. 10. Relation between  $\tau$  and  $I_i/I_o$  for  $H_{\text{spl}} = 20.1$  G and  $\Delta H_{\text{msl}} = 2.59$  G ( $r=0.125$ ) (solid line) and for  $H_{\text{spl}} = 8.1$  G and  $\Delta H_{\text{msl}} = 2.67$  G ( $r=0.33$ ) (dotted line).

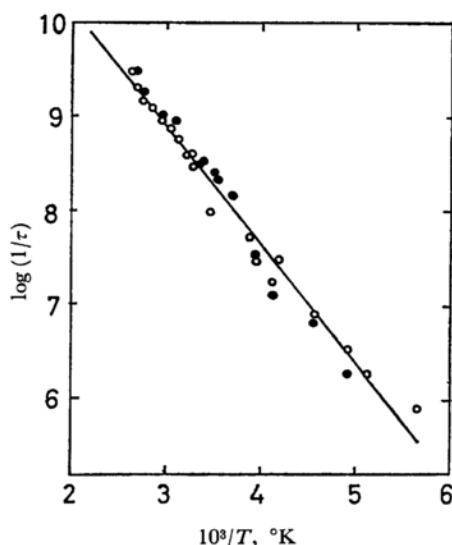


Fig. 11. Arrhenius plot of  $1/\tau$  versus  $1/T$ . The straight line illustrates Eq. (3) with  $E=5.8$  kcal/mol and  $f_0=4.4 \times 10^{12} \text{ sec}^{-1}$ . (O:  $H_{\text{spl}}=20.1$  G,  $\Delta H_{\text{msl}}=2.59$  G, ●:  $H_{\text{spl}}=8.1$  G,  $\Delta H_{\text{msl}}=2.67$  G)

for the case of  $r=0.33$ . The ratios  $I_i/I_o$  calculated for  $r=0.125$  and  $r=0.33$  are shown in Fig. 10 as functions of  $\tau$ . Comparing the quantities  $I_i/I_o$  observed at various temperatures with the calculated values,  $\tau$  has been determined for the temperatures at which the spectra were obtained. The plots of  $\log(1/\tau)$  versus  $1/T$  are shown in Fig. 11. The linear relation between  $\log(1/\tau)$  and  $1/T$  indicates that  $\tau$  follows the equation;

$$\frac{1}{\tau} = f_0 \exp(-E/RT), \quad (3)$$

where  $f_0$  and  $E$  are interpreted as the frequency factor and activation energy for the rotation of the  $\text{CH}_2$  group about the  $\text{C}_1\text{-C}_2$  bond, respectively.



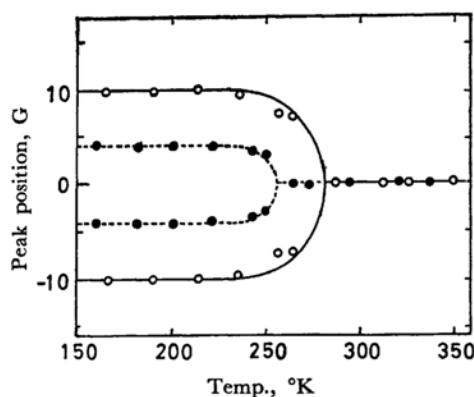


Fig. 12. Observed (dots) and calculated (lines) positions of the inner line peaks of the absorption spectra of  $\text{CH}_2\text{COO}^-$  in a zinc acetate dihydrate single crystal with varying temperature. The peak positions from the center of the spectra are measured in Gauss.

(○, —: for  $H_{\text{spl}}=20.1$  G and  $\Delta H_{\text{msl}}=2.59$  G,  
●, ----: for  $H_{\text{spl}}=8.1$  G and  $\Delta H_{\text{msl}}=2.67$  G)

The values for  $E$  and  $f_0$  are found from Arrhenius plots in Fig. 11 as:

$$\left. \begin{aligned} E &= 5.8 \pm 0.2 \text{ kcal/mol} \\ f_0 &= (4.4 \pm 2.7) \times 10^{12} \text{ sec}^{-1} \end{aligned} \right\} \quad (4)$$

In Figs. 5 and 6 the spectra calculated by Eqs. (2), (3) and (4) are illustrated with dotted lines for given temperatures. These figures show that the calculated spectra are in good agreement with the observed ones except tail parts of the absorption lines. The position of the inner line peaks has been calculated by the similar procedure as before and compared with the observation (Fig. 12). It is found in Fig. 12 that the observation is in good agreement with the calculation. The value of the frequency factor  $f_0$  given in (4) is also in good agreement with  $5.2 \times 10^{12} \text{ sec}^{-1}$  which is evaluated by the equation  $f_0 = kT/h$  based on the absolute rate theory,<sup>17</sup> where  $T$  is assumed to be 250°K. Lefebvre and Maruani<sup>18</sup> have calculated the absorption and first derivative spectra of randomly oriented  $\text{CH}_2\text{COOH}$  in which the methylene group rotate freely or is completely quenched around the C-C bond (see Fig. 13 of their paper). It can be seen that Fig. 13 of their paper also reproduces the first derivative curves of the irradiated zinc acetate dihydrate powder (Fig. 7) in fair detail.

Disagreement of the calculated curves with the observed ones in the tail region (Figs. 5 and 6) arises from the following two reasons. Firstly, the calculation was carried out with an assumption

that the shape function of each absorption line is Lorentzian but the real absorption line was nearly Gaussian. Secondly, the second-order effect or the "forbidden" transition was not taken into account, which was caused by a simultaneous transition of electronic and nuclear spins, though it was really observed in both sides of the absorption lines, as seen in Figs. 5 and 6.

For such radicals as  $\text{CH}_2\text{NHCONH}_2$  (from methylurea),<sup>19</sup>  $\text{CF}_2\text{CONH}_2$  (from trifluoroacetamide)<sup>20</sup> and  $\text{CH}_2\text{COOH}$  (from malonic acid),<sup>15</sup> the rotation of the  $\text{CH}_2$  or  $\text{CF}_2$  group does not occur even at room temperature. Activation energy of these groups is estimated to be higher than 9 kcal/mol. If it is assumed that  $f_0 = 5 \times 10^{12} \text{ sec}^{-1}$  and  $H_{\text{spl}}=10$  G, the lower energy than 9 kcal/mol would reveal the effect of the rotation on their ESR spectra. Therefore, it is of interest to examine, using a simple model, the cause of the fairly low activation energy for the  $\text{CH}_2$  rotation in the case of  $\text{CH}_2\text{COO}^-$  in a crystal of zinc acetate dihydrate.

Now, we define  $\theta$  as the angle between the plane  $\text{H}_1\text{C}_1\text{H}_2$  and the plane  $\text{O}_1\text{O}_2\text{C}_2$ , and consider only an internal energy  $V(\theta)$  of the radical which is a function of  $\theta$ .  $V(\theta)$  is a sum of the energies of five  $\pi$ -electrons  $V_\pi(\theta)$  plus a repulsive energy  $V_r(\theta)$  between the  $\text{CH}_2$  and  $\text{COO}^-$  groups;

$$V(\theta) = V_\pi(\theta) + V_r(\theta). \quad (5)$$

$V_\pi(\theta)$  will be minimum at  $\theta=0$  and  $\pi$ , and maximum at  $\theta=\pi/2$  and  $3\pi/2$ , whereas  $V_r(\theta)$  is maximum at  $\theta=0$  and  $\pi$ , and minimum at  $\theta=\pi/2$  and  $3\pi/2$ . The activation energy  $E$  for the rotation may be approximately  $V(\pi/2) - V(0)$ . With the simple Hückel MO method  $V_\pi(\pi/2) - V_\pi(0)$  was calculated as follows.<sup>21</sup> Taking Coulomb energy for  $\text{C}_1$ ,  $\text{C}_2$ ,  $\text{O}_1$  and  $\text{O}_2$  to be  $\alpha$ ,  $\alpha+0.2\beta$ ,  $\alpha+2\beta$ , and  $\alpha+2\beta$ , respectively, and taking the resonance energy for the  $\text{C}_1\text{-C}_2$ ,  $\text{C}_2\text{-O}_1$  and  $\text{C}_2\text{-O}_2$  bonds to be  $\beta \cos \theta$ ,  $\sqrt{2}\beta$  and  $\sqrt{2}\beta$ , respectively, it is found that  $V_\pi(\pi/2) - V_\pi(0) = -0.562\beta$ . If  $\beta$  is taken as  $-18$  kcal/mole,<sup>21</sup> which have been evaluated from the resonance energy for benzene,  $V_\pi(\pi/2) - V_\pi(0)$  is 10.1 kcal/mol.

$V_r(\theta)$  is not known experimentally, but  $V_r(0) - V_r(\pi/2)$  can be roughly evaluated as follows. Assuming the repulsive energy between a hydrogen atom and an oxygen atom is the same in  $\text{CH}_2\text{COO}^-$  and  $\text{CH}_3\text{COOH}$ , the activation energy for the hindered rotation of  $\text{CH}_2\text{COO}^-$  may be larger than that of the methyl group in  $\text{CH}_3\text{COOH}$ , which has been known to be  $2.5 \pm 0.7$  kcal/mol.<sup>22</sup>

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This is because the height of two fold potential barrier (in the case of  $\text{CH}_2\text{COO}^-$ ) is larger than that of three fold potential barrier (in the case of  $\text{CH}_3\text{COOH}$ ). Thus,  $V_r(0) - V_r(\pi/2)$  may be estimated without serious error as twice the activation energy for  $\text{CH}_3\text{COOH}$ , *i. e.*,  $5.0 \pm 1.4$  kcal/mol. Therefore, the activation energy for the rotation of  $\text{CH}_2$  in  $\text{CH}_2\text{COO}^-$  is  $V(\pi/2) - V(0) = 10.1 - (5.0 \pm 1.4)$  kcal/mol  $= 5.1 \pm 1.4$  kcal/mol, which is in good agreement with the observed value  $5.6 \pm 0.2$  kcal/mol.

The agreement of the calculated activation energy with the observation for  $\text{CH}_2\text{COO}^-$  in

a crystal of zinc acetate dihydrate suggests that the contribution of the surrounding molecules to the hindered rotation of the  $\text{CH}_2$  group is negligibly small and that the activation energy is essentially determined by the internal energy of the radical. For the radicals of the type  $\text{CH}_2\text{R}$  having a high activation energy, however, the rotation of the  $\text{CH}_2$  group may be hindered by the force acting on the radicals from the surrounding molecules in the crystals.

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